



# School of Modern Optics

9 May 2013, Puebla, Mexico

## Lecture 4

# Optical vortex generation using liquid crystals II

Etienne Brasselet

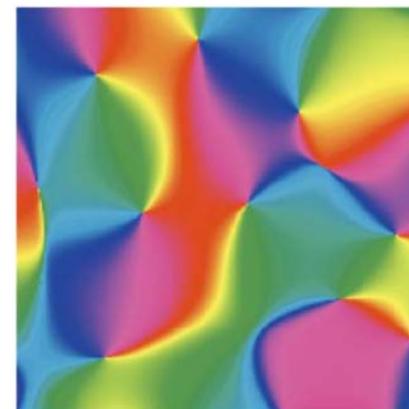
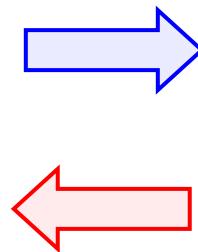
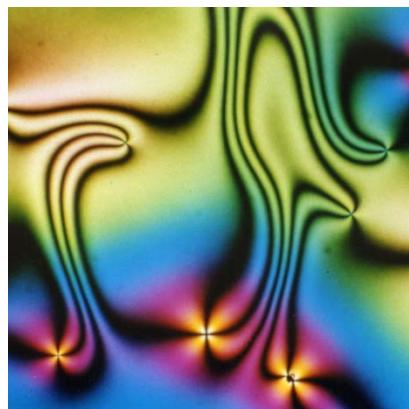
*Singular Optics & Liquid Crystals group*

[www.loma.cnrs.fr/spip.php?rubrique331](http://www.loma.cnrs.fr/spip.php?rubrique331)

Laboratoire Ondes et Matières d'Aquitaine  
CNRS, Université Bordeaux 1, France

## Imprinting material topological information on light

Liquid crystal  
defects



Optical phase  
singularities

## Imprinting optical topological information on matter

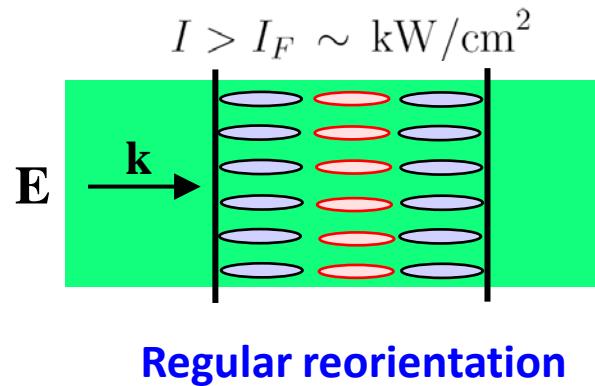
# Outline

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- 1. Light-induced liquid crystals topological defects**
2. On-demand optical vortex generation
3. Nonlinear spin-orbit optical phenomena
4. Reconfigurable metastable light-induced vortex arrays

## Optical reorientation of liquid crystals

1980 Optical Fréedericksz transition : a “regular” manifestation of the optical torque



A. S. Zolot'ko et al., JETP Lett. **32**, 158 (1980)

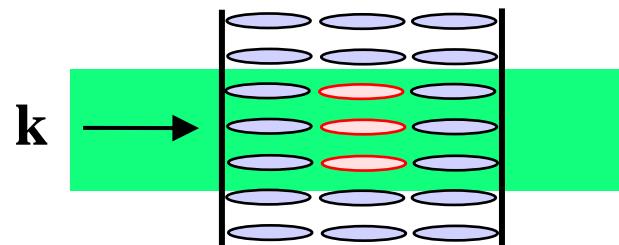
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30 years of studies (effects of : geometry, polarization, dopants, beam size, ...)

2009 Original geometry revisited



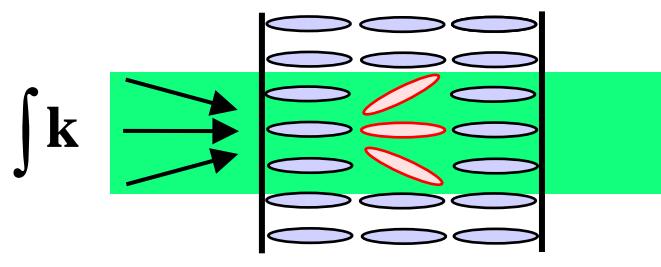
# Optical reorientation of liquid crystals

1980 Optical Fréedericksz transition : a “regular” manifestation of the optical torque



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2009 Original geometry revisited: a “singular” manifestation of the optical torque

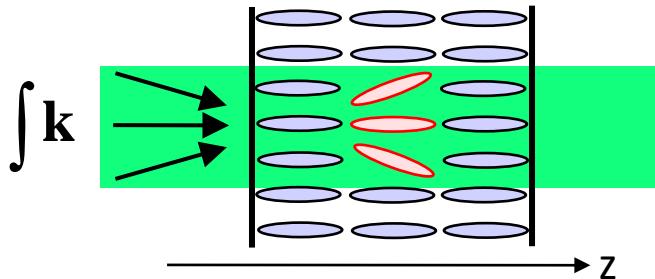


$$\Delta\mathbf{r} \cdot \Delta\mathbf{k} \neq 0$$

Topological optical reorientation

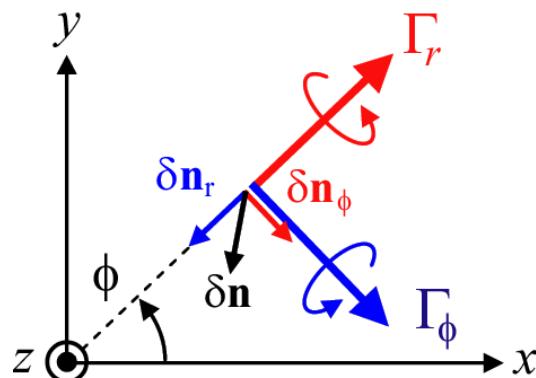
E. Brasselet, Opt. Lett. **34**, 3229 (2009) ; E. Brasselet, J. Opt. **12**, 124005 (2010)

## Topological optical reorientation : qualitative features



### Optical torque density

$$\begin{aligned}\Gamma &= \frac{1}{2} \epsilon_0 \epsilon_a \operatorname{Re}[(\mathbf{n} \cdot \mathbf{E}^*) (\mathbf{n} \times \mathbf{E})] \\ &= \frac{1}{2} \epsilon_0 \epsilon_a \operatorname{Re}(-E_z^* E_\phi \mathbf{e}_r + E_z^* E_r \mathbf{e}_\phi) \\ &= \boxed{\Gamma_r \mathbf{e}_r} + \boxed{\Gamma_\phi \mathbf{e}_\phi}\end{aligned}$$



# Topological optical reorientation : optical singularity at work ?

Let us consider a Gaussian beam under paraxial approximation

$$\mathbf{E}_\perp = E_0 u(r, z) \exp[-i(\omega t - kz)] \mathbf{e}_\perp$$

with

$$u(r, z) = \frac{w_0}{w(z)} \exp \left[ -\frac{r^2}{w^2(z)} + i \frac{kr^2}{2z(1 + z_0^2/z^2)} - i \arctan(z/z_0) \right]$$

The longitudinal field is usually neglected ... but can be calculated anyway !

$$\begin{aligned} \nabla \cdot \mathbf{E} = 0 &\Rightarrow \partial_z E_z = -\nabla_\perp \cdot \mathbf{E}_\perp \\ &\Rightarrow E_z = \frac{i}{k} \nabla_\perp \cdot \mathbf{E}_\perp + o(1/kw) \end{aligned}$$

Circular polarization case

$$\mathbf{e}_\perp = \mathbf{e}_\sigma = \frac{\mathbf{e}_x + i\sigma \mathbf{e}_y}{\sqrt{2}} , \sigma = \pm 1$$

$$\mathbf{E}_z = -\frac{i}{z_0 + iz} \frac{r}{\sqrt{2}} e^{i\sigma\phi} (\mathbf{E}_\perp \cdot \mathbf{e}_\sigma^*) \mathbf{e}_z$$

# Topological optical reorientation : optical singularity at work ?

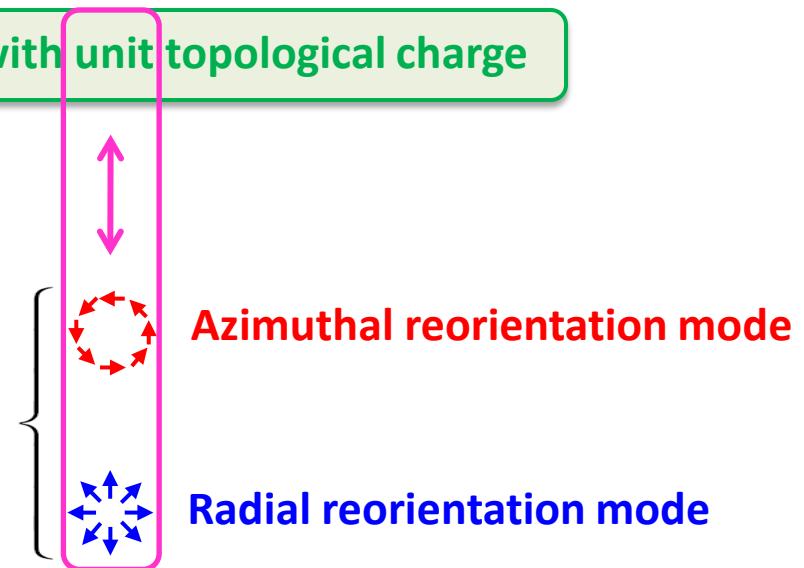
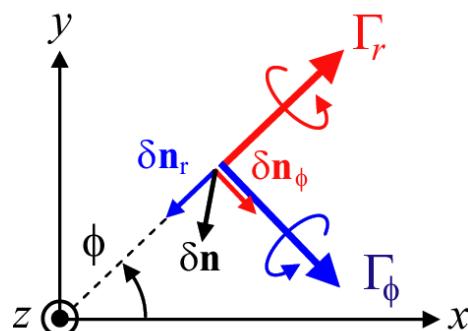
Total field for circular polarization state

$$\mathbf{E} = E_0 u(r, z) \exp[-i(\omega t - kz)] \left( \mathbf{e}_\sigma - \frac{i}{z_0 + iz} \frac{r}{\sqrt{2}} e^{i\sigma\phi} \mathbf{e}_z \right)$$

Spin angular momentum

Orbital angular momentum

Longitudinal optical vortex with unit topological charge

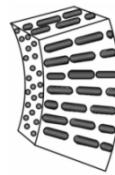


# Topological optical reorientation : a model

## Total free energy minimization

$$\mathcal{F} = \int_0^L \int_0^\infty \int_0^{2\pi} r(F_{\text{el}} + F_{\text{opt}}) d\phi dr dz$$

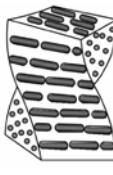
Elastic distortion modes



Splay



Bend



Twist

Maxwell's equations

Paraxial solution in c-cut anisotropic media

A. Ciattoni *et al.*, JOSA B **18**, 156 (2001)

A. Ciattoni *et al.*, JOSA A **20**, 163 (2003)

E. Brasselet *et al.*, Opt. Lett. **34**, 1021 (2009)

## Ansatz for singular reorientation modes

$$\delta \mathbf{n} = \delta n_r \mathbf{e}_r + \delta n_\phi \mathbf{e}_\phi + \delta n_z \mathbf{e}_z \quad \text{with} \quad \delta n_z = (1 - \delta n_r^2 - \delta n_\phi^2)^{1/2} - 1$$

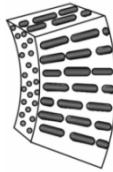
$$\text{Axial symmetry : } \partial \Gamma_{r,\phi} / \partial \phi = 0 \quad \Leftrightarrow \quad \delta n_{r,\phi} = \mathcal{R}(r) \mathcal{Z}(z)$$

# Topological optical reorientation : a model

## Total free energy minimization

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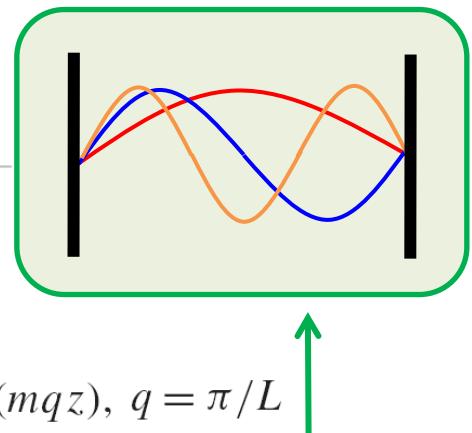
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Ansatz for singular reorientation modes

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Axial symmetry :  $\partial \Gamma_{r,\phi} / \partial \phi = 0 \Rightarrow \delta n_{r,\phi} = \mathcal{R}(r) \mathcal{Z}(z)$

Longitudinal boundary conditions :  $\mathcal{Z}(0, L) = 0 \Rightarrow \mathcal{Z}(z) = \sum_m A^{(m)} \sin(mqz), q = \pi/L$

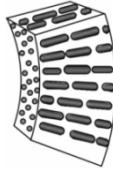


# Topological optical reorientation : a model

## Total free energy minimization

$$\mathcal{F} = \int_0^L \int_0^\infty \int_0^{2\pi} r(F_{\text{el}} + F_{\text{opt}}) d\phi dr dz$$

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$$\mathbf{E} = E_0 u(r, z) \exp[-i(\omega t - kz)] \left( \mathbf{e}_\sigma - \frac{i}{z_0 + iz} \frac{r}{\sqrt{2}} e^{i\sigma\phi} \mathbf{e}_z \right)$$

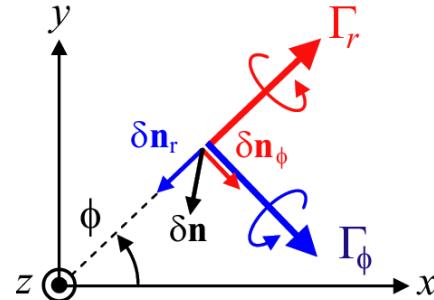
Axial symmetry :  $\partial \Gamma_{r,\phi} / \partial \phi = 0 \Rightarrow \delta n_{r,\phi}$

Longitudinal boundary conditions :  $\mathcal{Z}(0, L) = 0 \Rightarrow \mathcal{Z}(z) = \sum_m A^{(m)} \sin(mqz), q = \pi/L$

Transverse boundary conditions :  $\mathcal{R}(0, \infty) = 0 \Rightarrow \underline{\mathcal{R}(r) = (r/w) \exp(-2r^2/w^2)}$

# Topological optical reorientation : a model

## Ansatz for singular reorientation modes



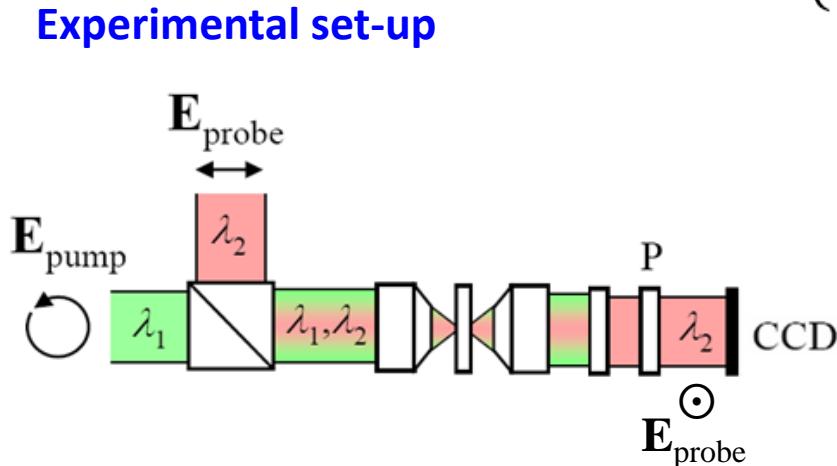
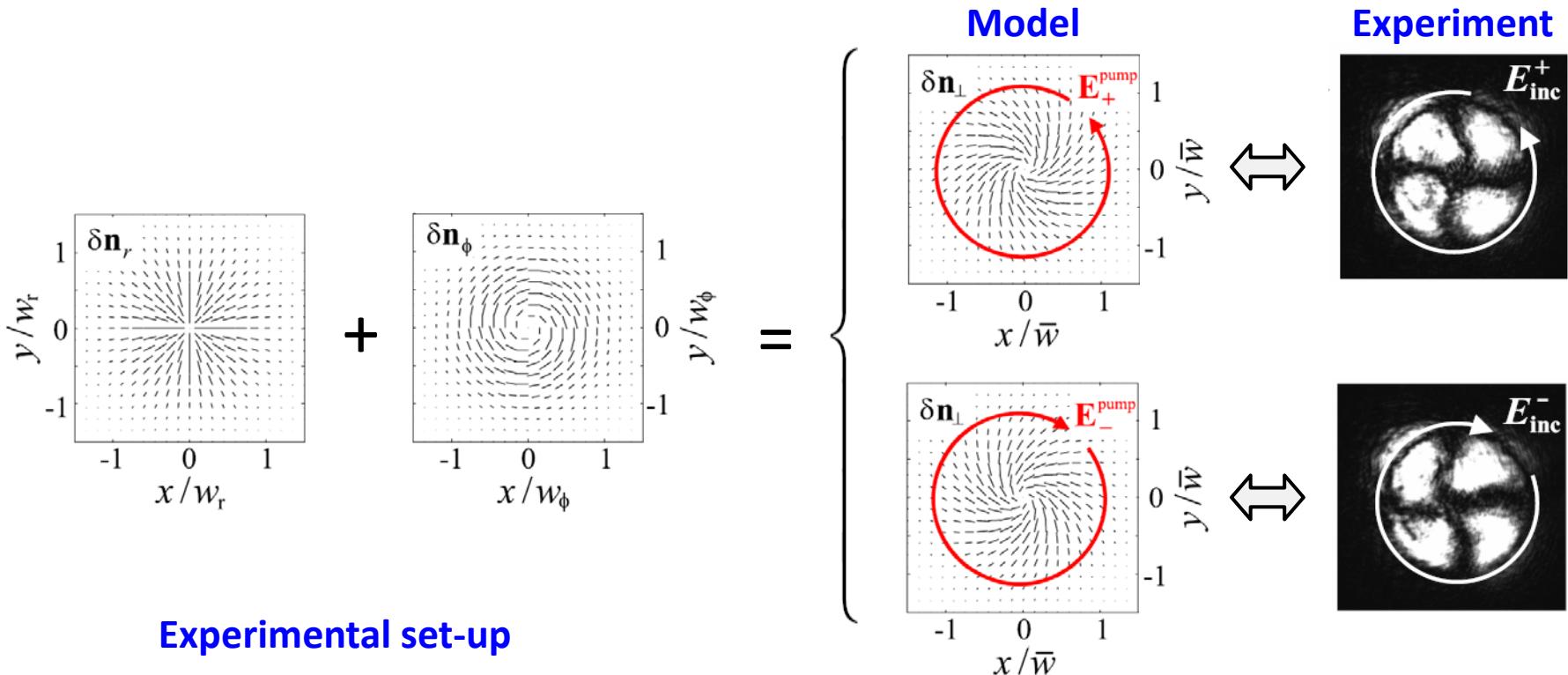
$$\delta n_{r,\phi}(r, z) = \frac{r}{w_{r,\phi}} \exp(-2r^2/w_{r,\phi}^2) \sum_m A_{r,\phi}^{(m)} \sin(mqz)$$

Retaining only the first longitudinal mode (m=1)

$$\frac{\partial \mathcal{F}}{\partial u_k} = 0 , \quad \mathbf{u} = (A_r, A_\phi, w_r, w_\phi)$$

E. Brasselet, J. Opt. **12**, 124005 (2010)

# Topological optical reorientation : simulation / experiment

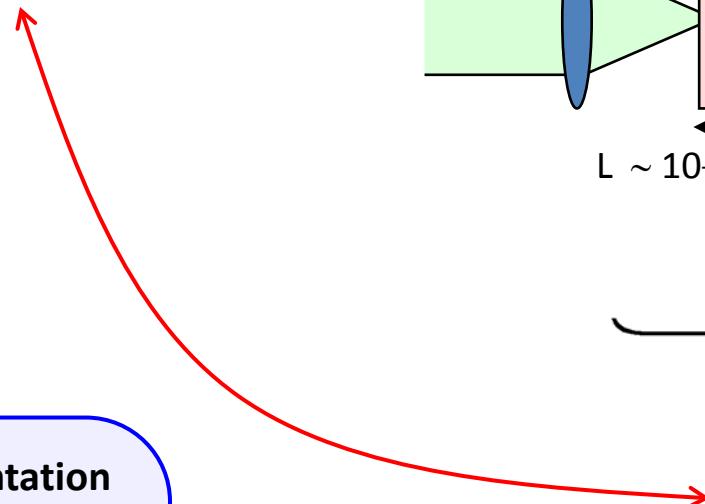


**Spin controlled  
Light-induced chiral elastic modes**

# Topological optical reorientation : why hidden for 30 years ?

## Theoretical reason

Plane wave is easier !



### Topological reorientation

$$\theta_0 \sim 100 \text{ mrad}$$

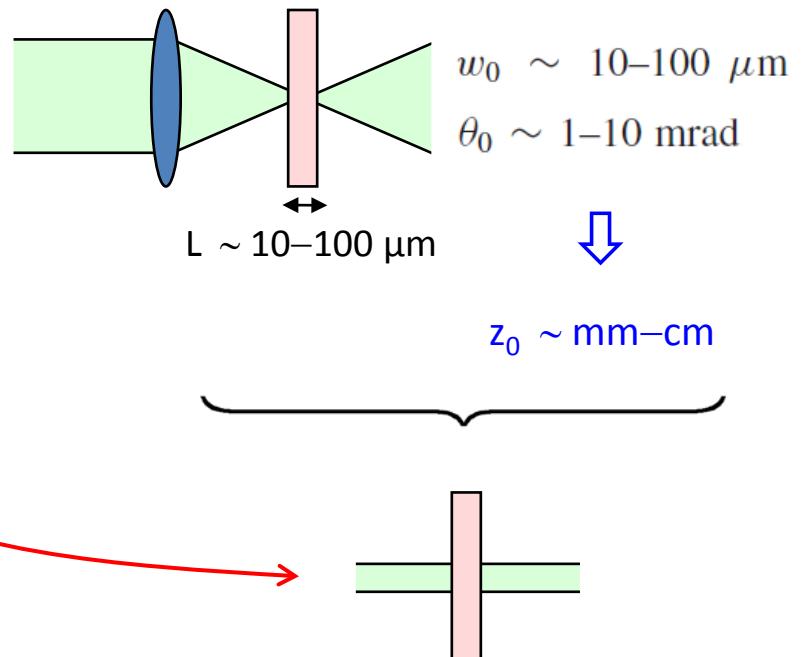


$$z_0 < L$$



Plane wave inappropriate

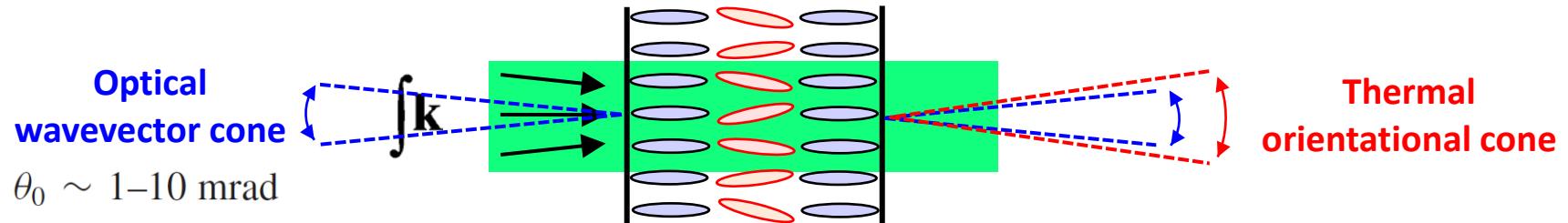
## Experimental reason



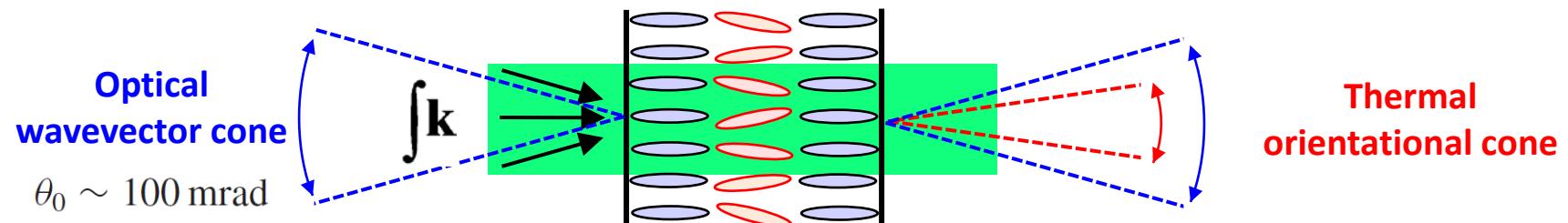
Cylindrical beam approximation

# Topological optical reorientation : why hidden for 30 years ?

## Regular collective reorientation



## Singular collective reorientation



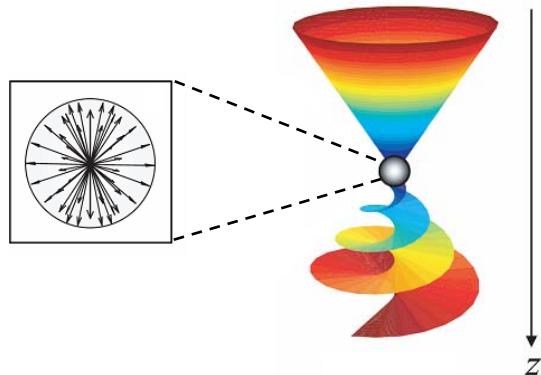
# Outline

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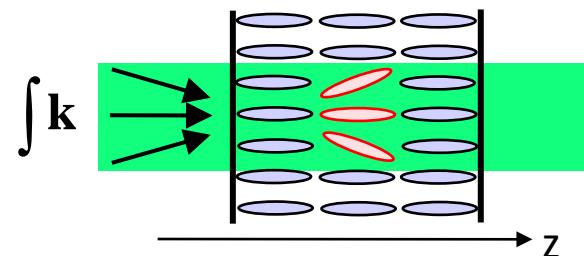
1. Light-induced liquid crystals topological defects
2. **On-demand optical vortex generation**
3. Nonlinear spin-orbit optical phenomena
4. Reconfigurable metastable light-induced vortex arrays

# On-demand optical vortex generation

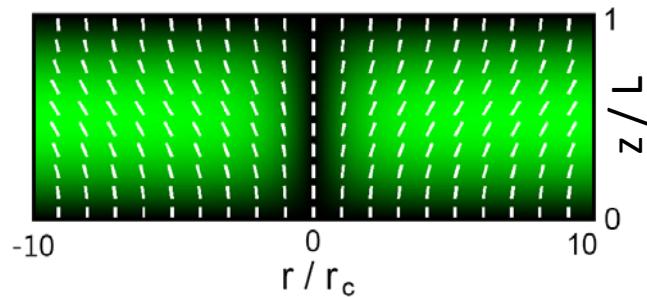
## 3D radial birefringence natural option



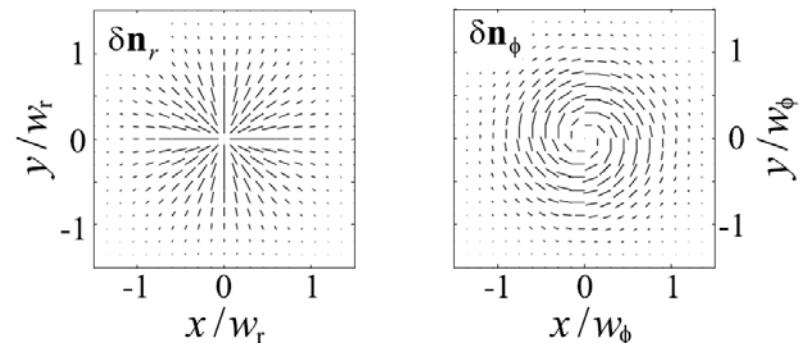
## Light-induced option : topological reorientation



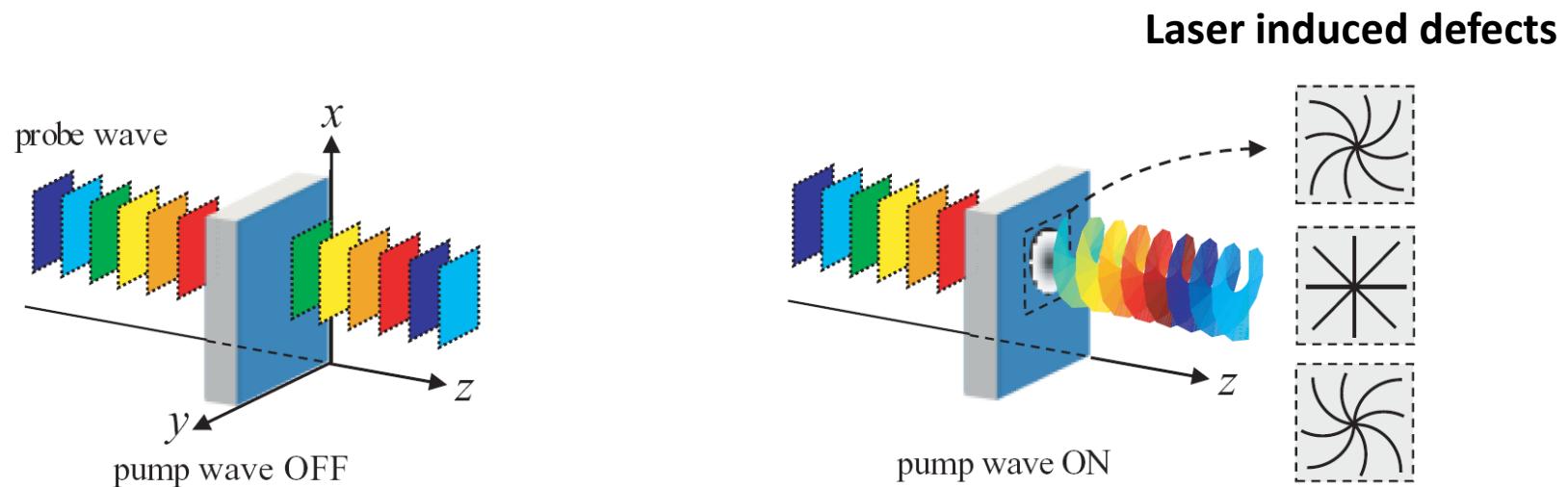
## Light-induced on-demand umbilical defects



## Flexible spin-orbit converters



## On-demand optical vortex generation : principle

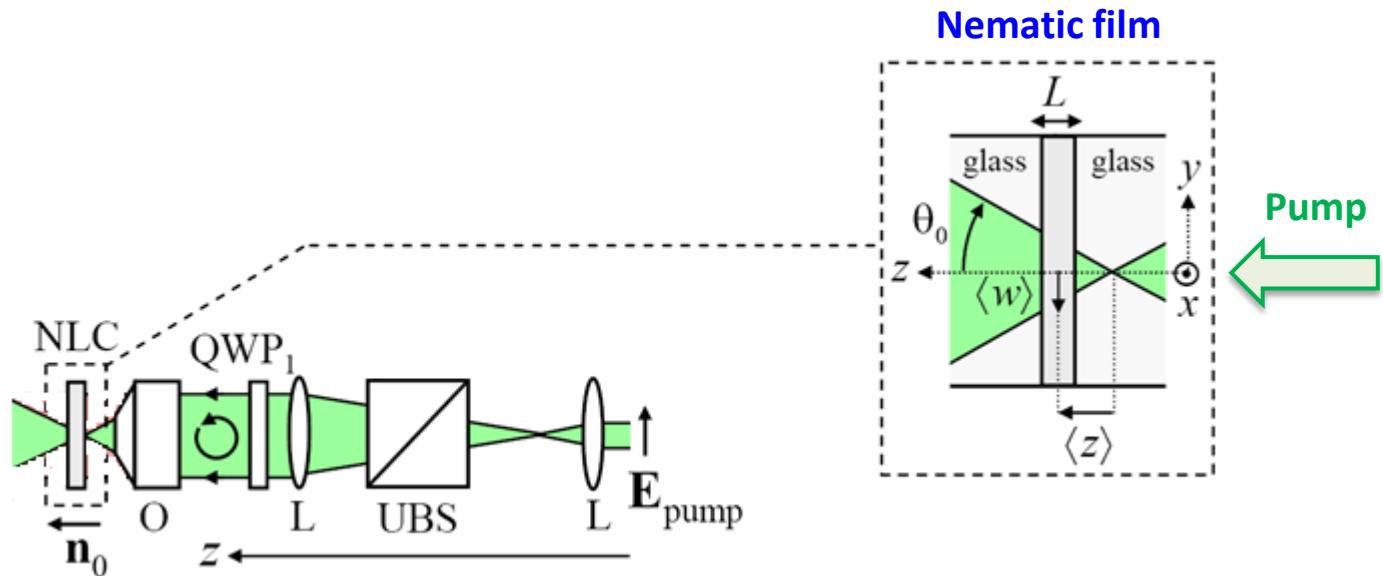


**On-demand local encoding of optical phase singularities**

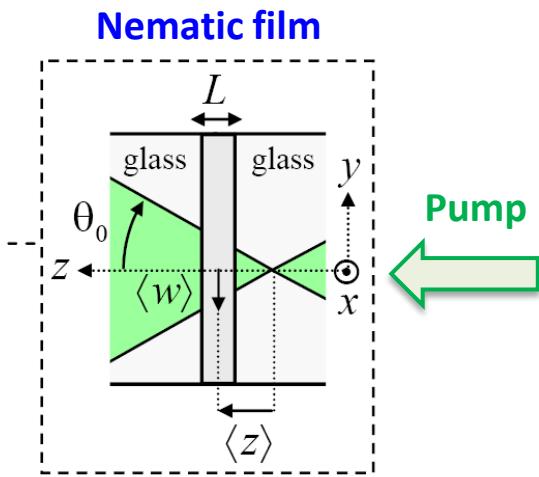
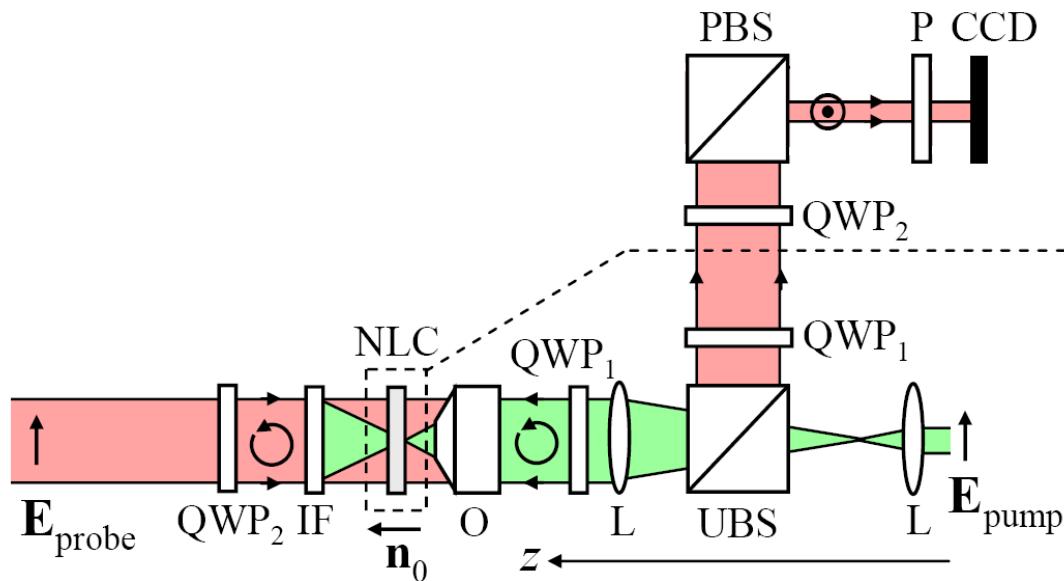
**Induced by light and mediated by matter**

E. Brasselet, PRA **82**, 063836 (2010)

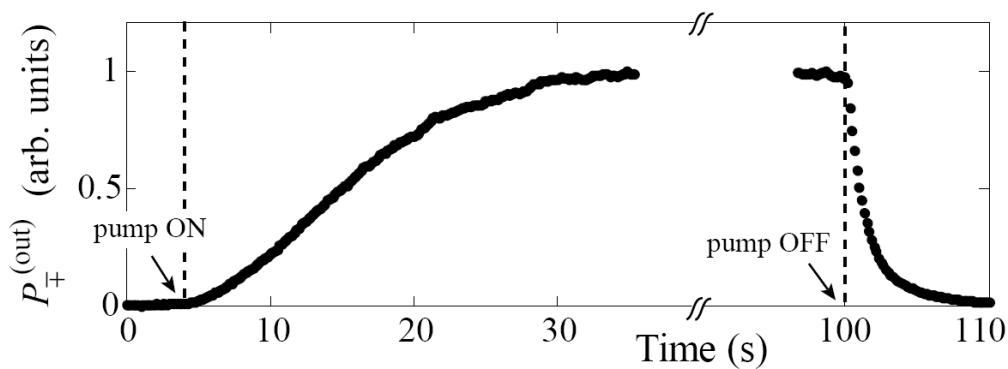
# On-demand optical vortex generation : the experiment



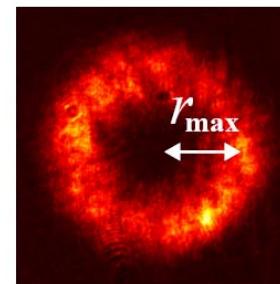
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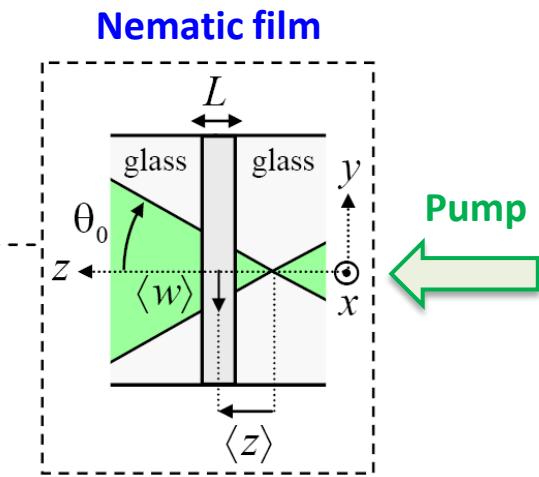
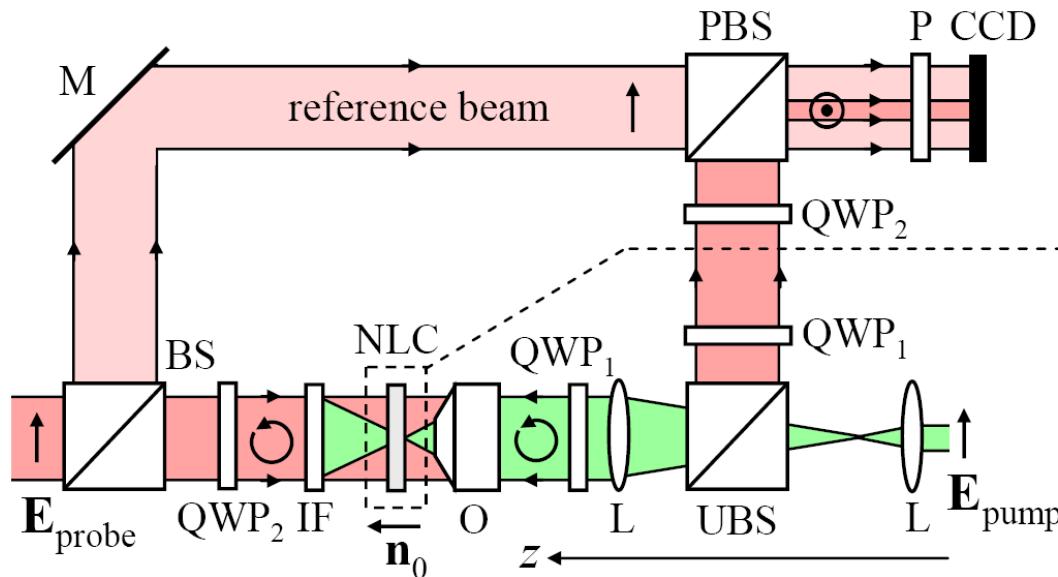
Rewritable process : writing-erasing cycle



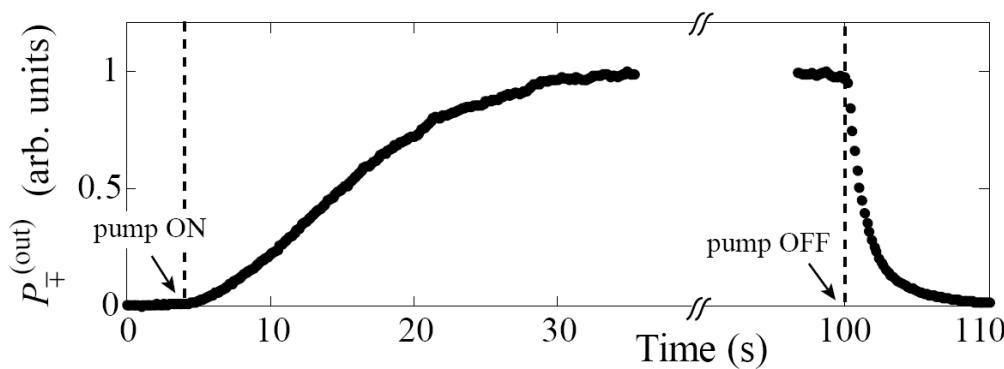
Steady vortex



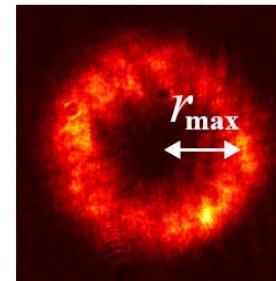
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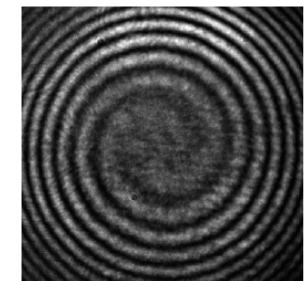
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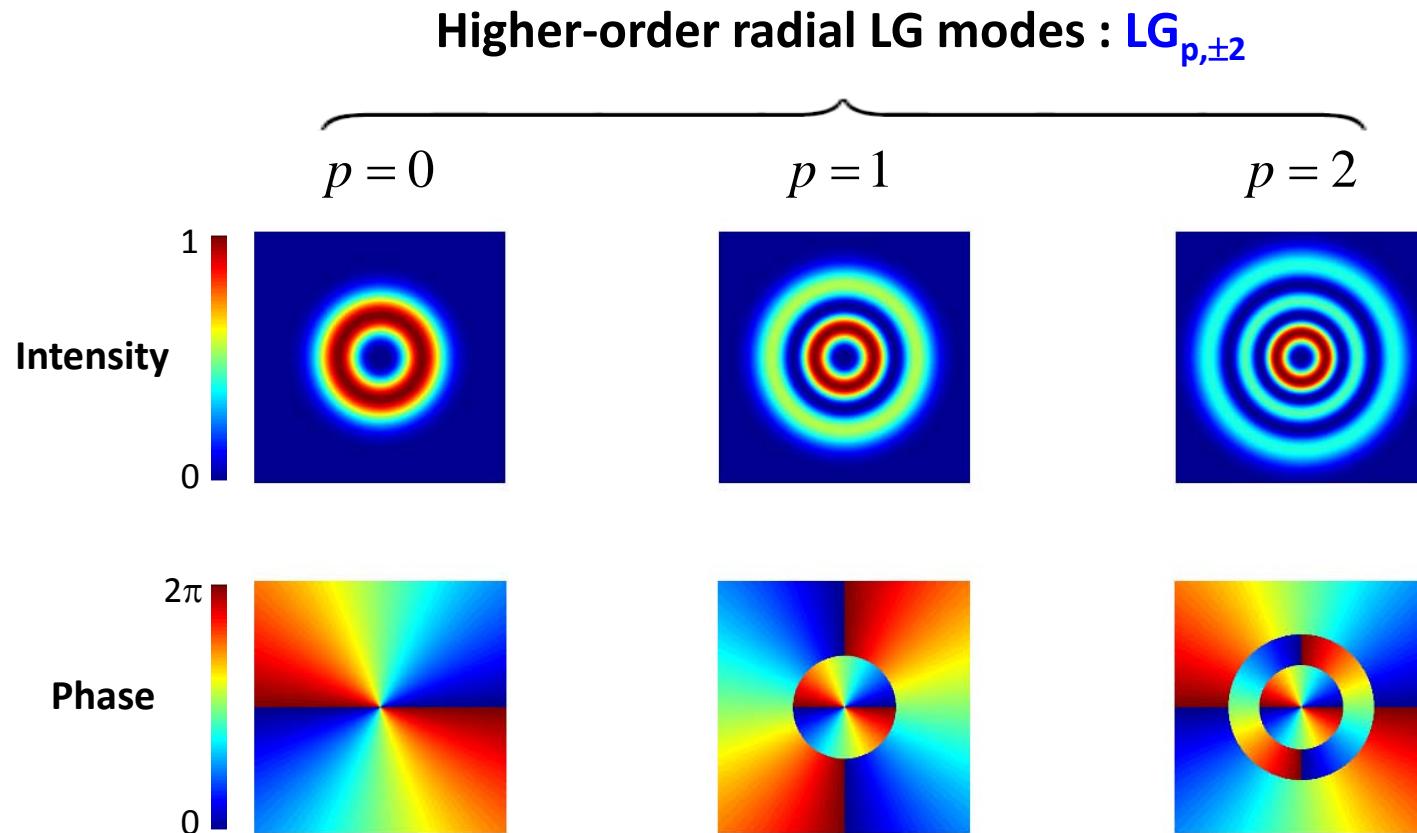
Steady vortex



Topological charge two

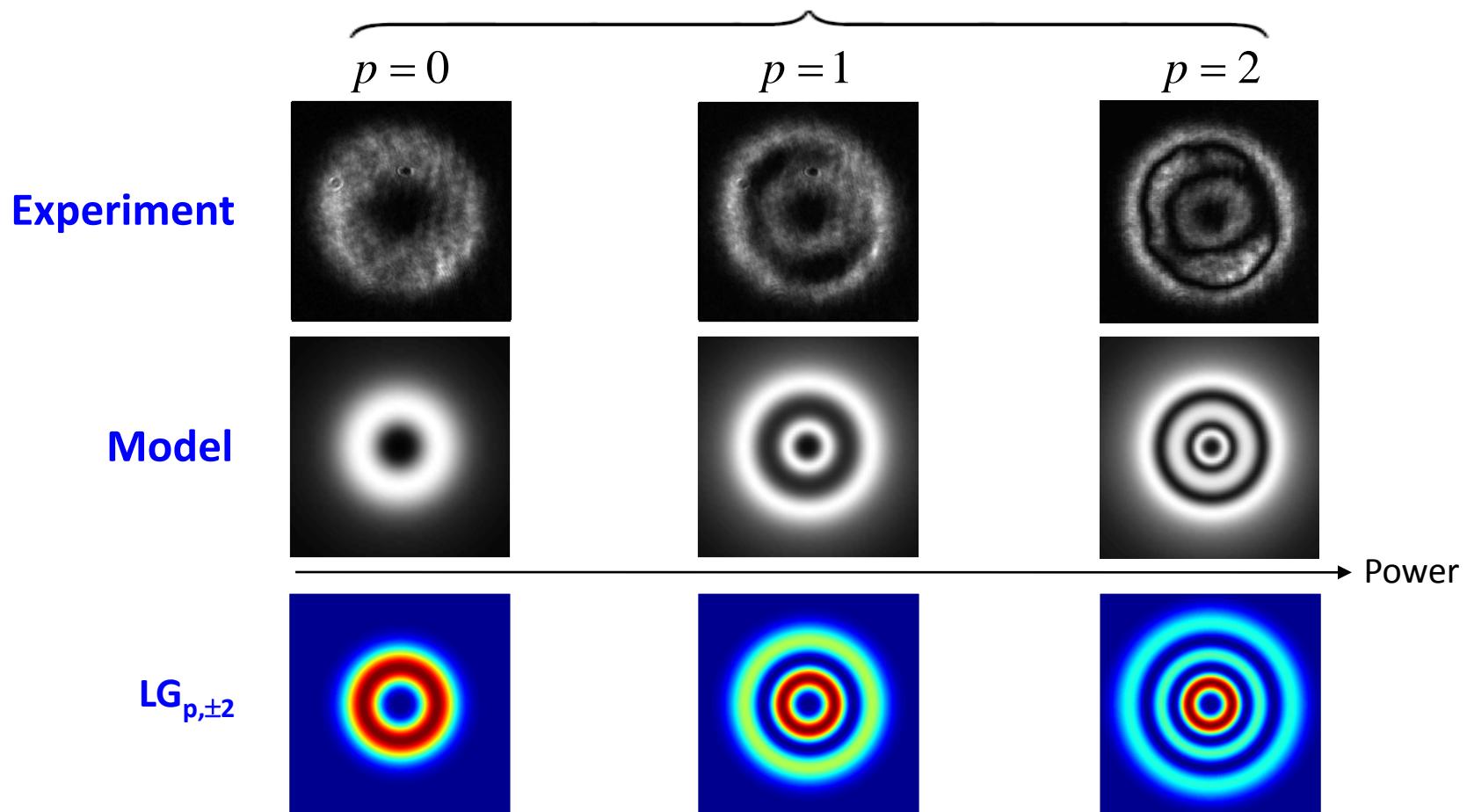


# Higher-order light-induced optical vortices ?



# Higher-order light-induced optical vortices ?

Different radial index : analogy with  $LG_{p,\pm 2}$  beams



What about self-induced effects ?

# Outline

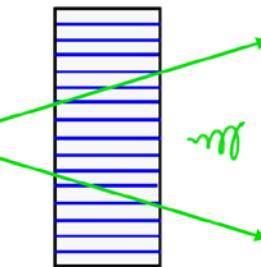
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1. Light-induced liquid crystals topological defects
2. On-demand optical vortex generation
- 3. Nonlinear spin-orbit optical phenomena**
4. Reconfigurable metastable light-induced vortex arrays

# From linear to nonlinear optical spin-orbit interaction

No defect  $\leftrightarrow$  Linear regime

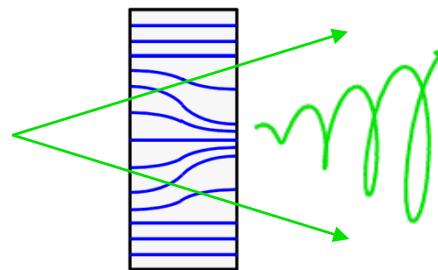
Circularly polarized Gaussian beam      Contra-circularly polarized vortex beam



What is the effect of a light-induced topological defect ?

Laser-induced defect  $\leftrightarrow$  Nonlinear regime

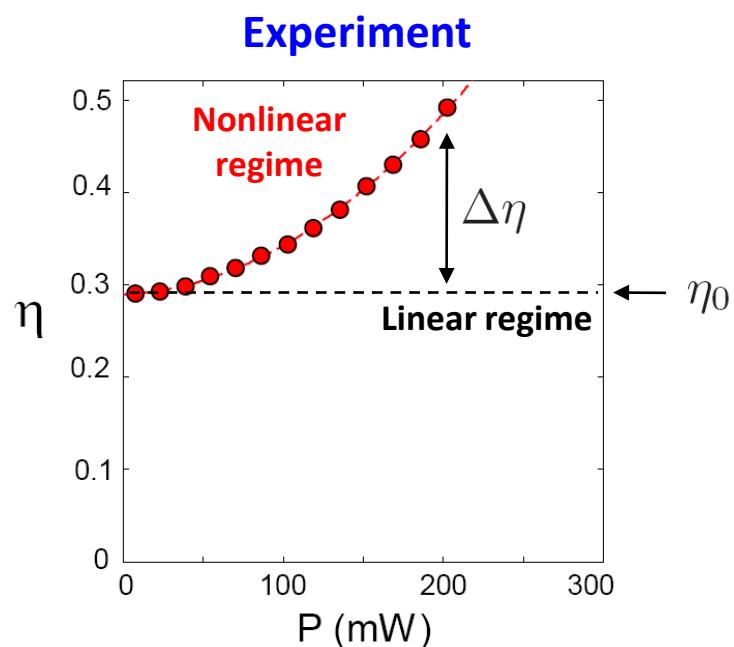
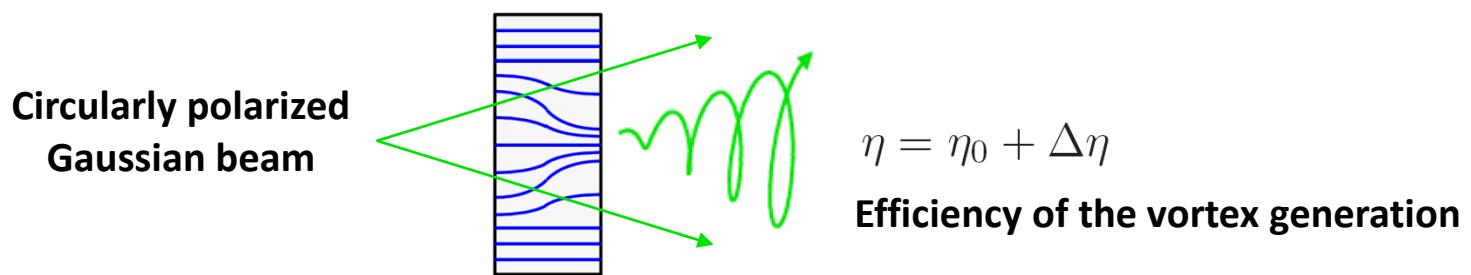
Circularly polarized Gaussian beam



# Self-induced spin-to-orbital angular momentum conversion

Nonlinear regime

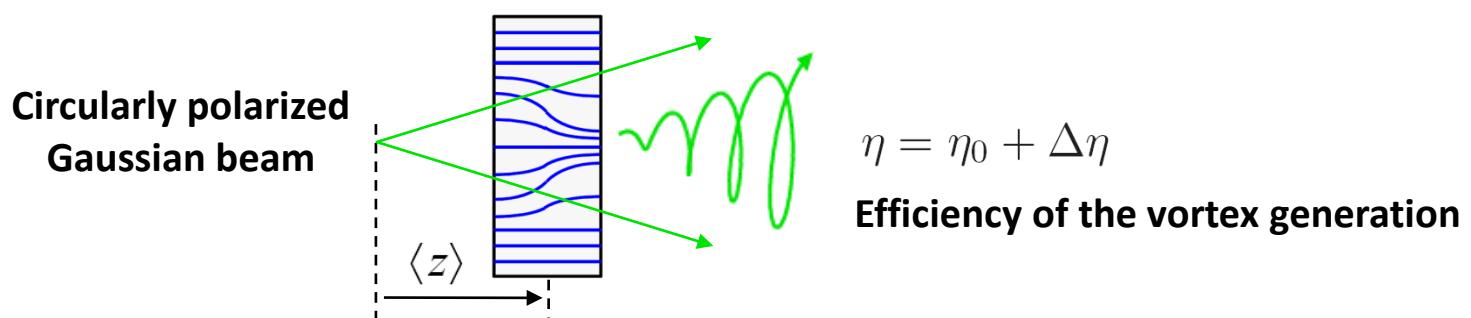
Topological optical reorientation at work



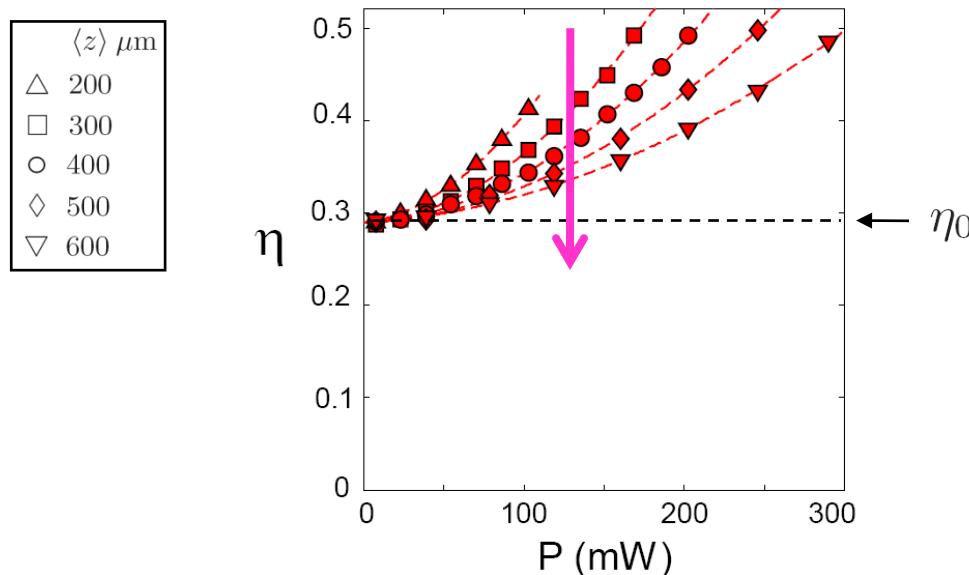
# Self-induced spin-to-orbital angular momentum conversion

Nonlinear regime

Topological optical reorientation at work



Experiment

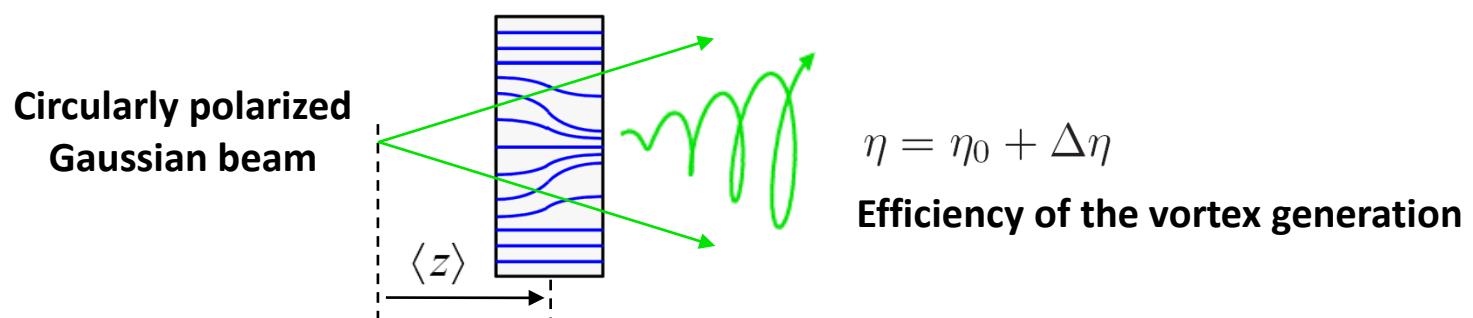


Beam spot increases  
↓  
Intensity decreases at fixed power

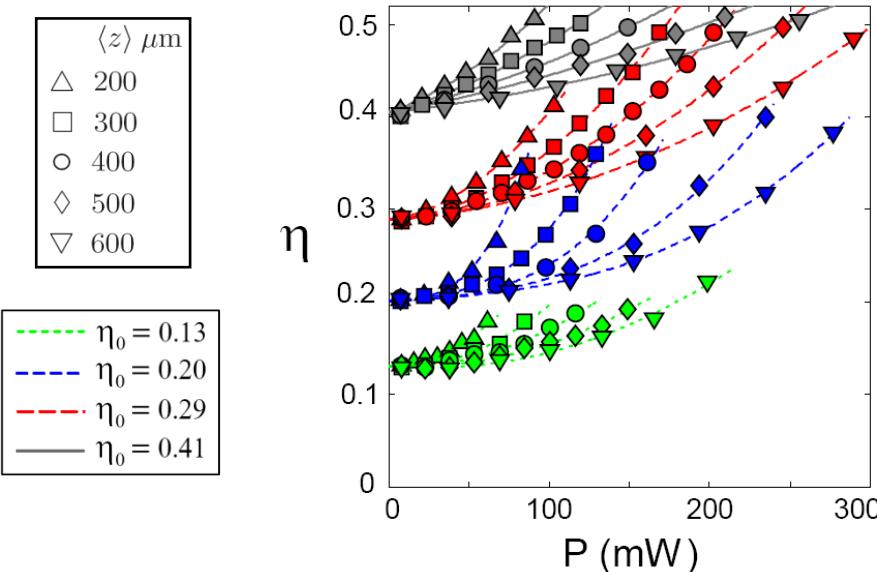
# Self-induced spin-to-orbital angular momentum conversion

Nonlinear regime

Topological optical reorientation at work



Experiment

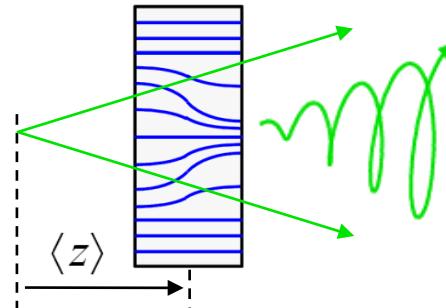


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Nonlinear regime

Topological optical reorientation at work

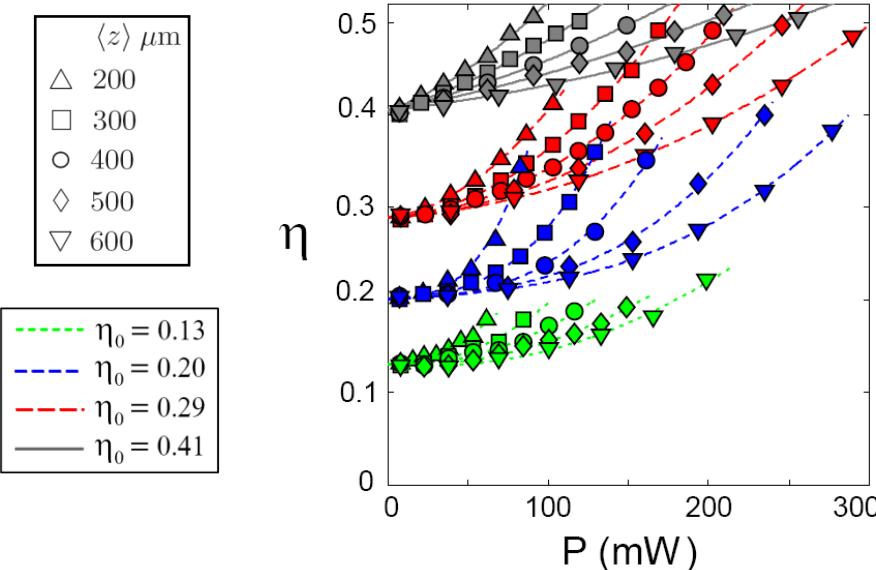
Circularly polarized  
Gaussian beam



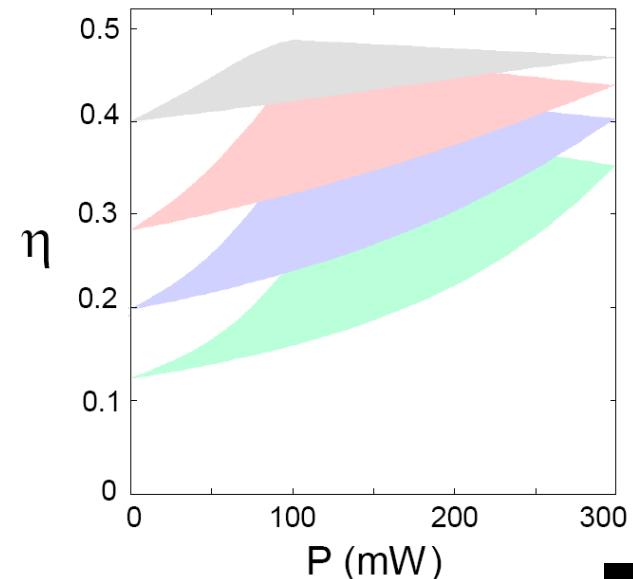
$$\eta = \eta_0 + \Delta\eta$$

Efficiency of the vortex generation

Experiment



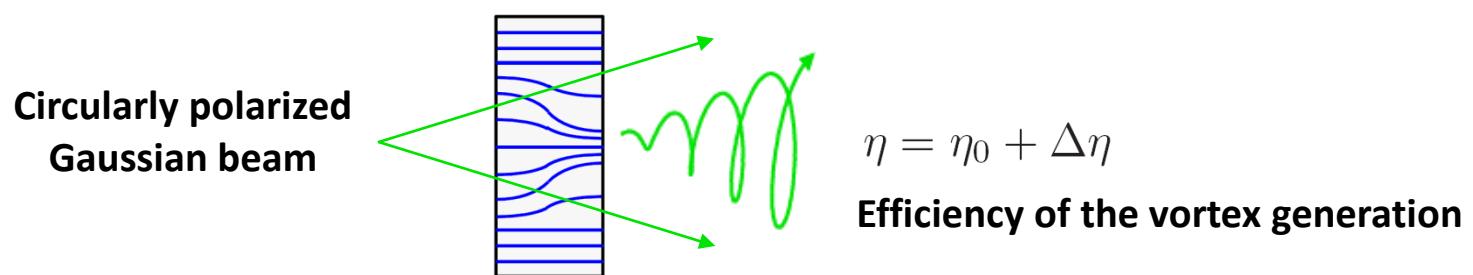
Model



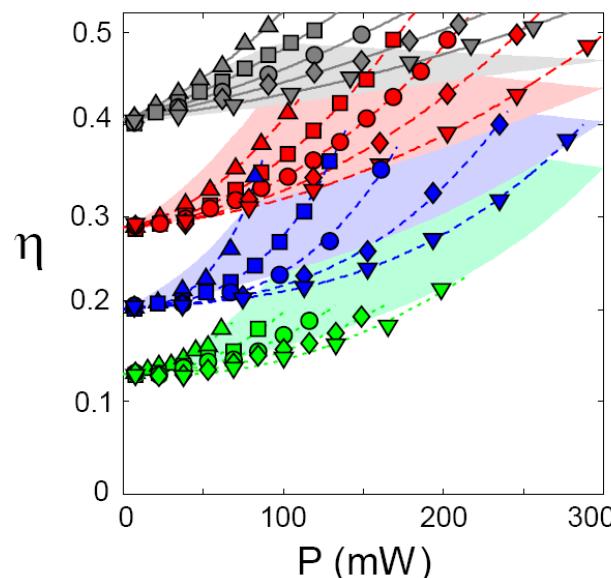
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Nonlinear regime

Topological optical reorientation at work

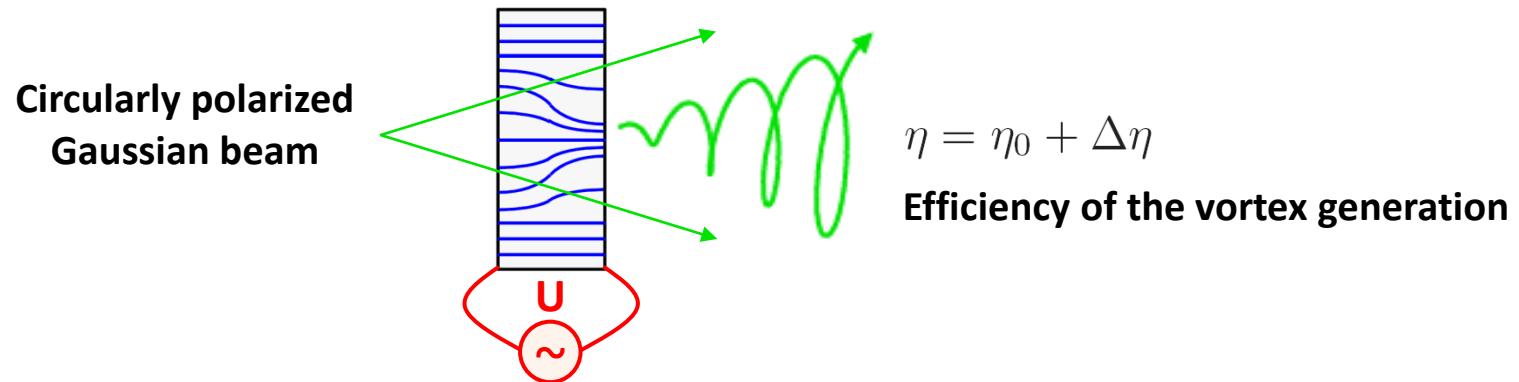


Experiment vs. Model

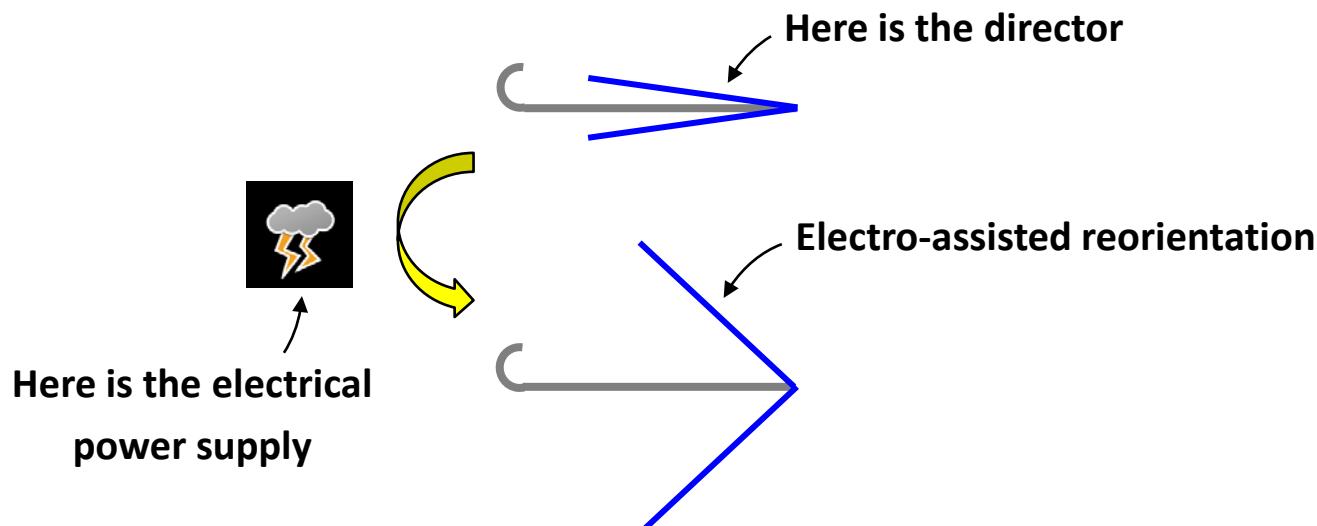


# Electrically enhanced nonlinear optical spin-orbit coupling

Enhanced nonlinearity using « negative nematics » ( $\varepsilon_a < 0$ )

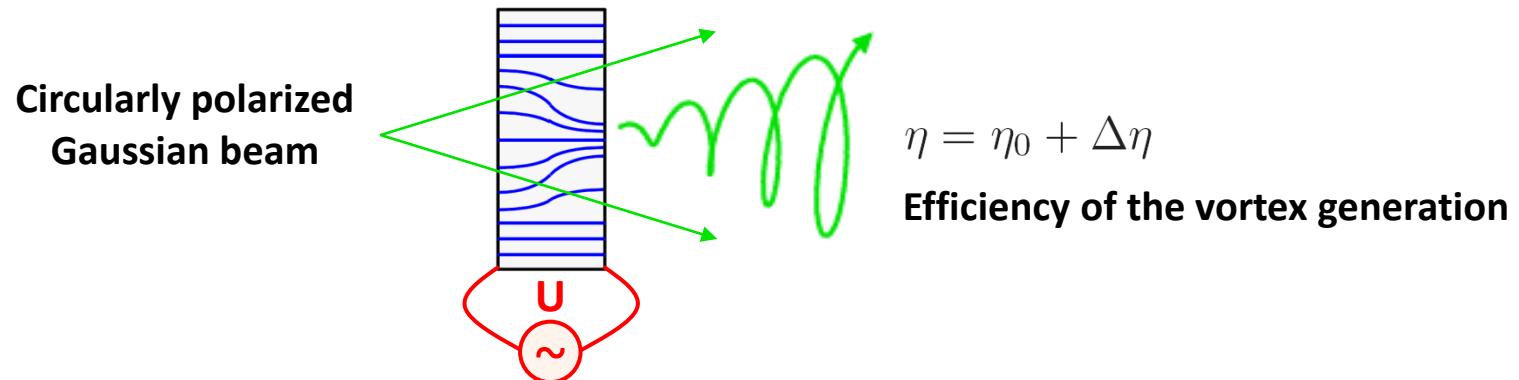


Opening of the « liquid crystal umbrella »

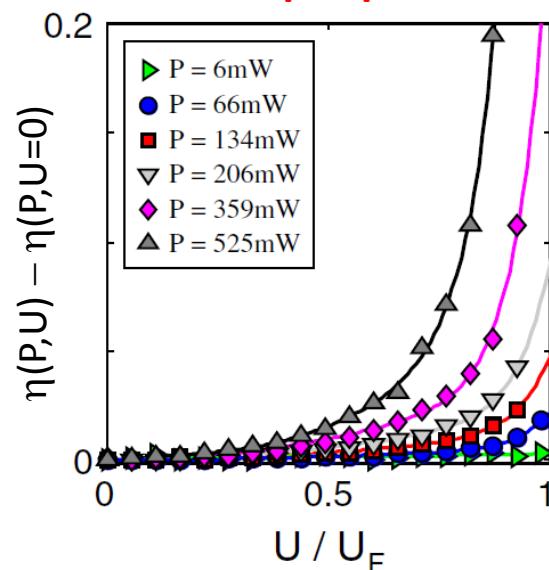


# Electrically enhanced nonlinear optical spin-orbit coupling

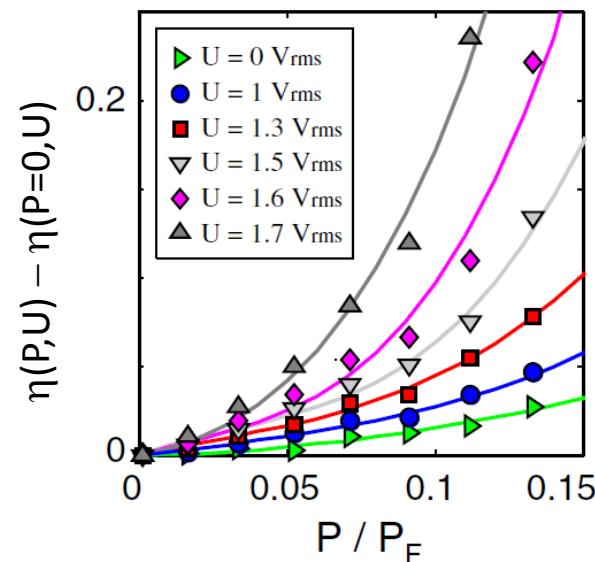
Enhanced nonlinearity using « negative nematics » ( $\varepsilon_a < 0$ )



Fixed input power P

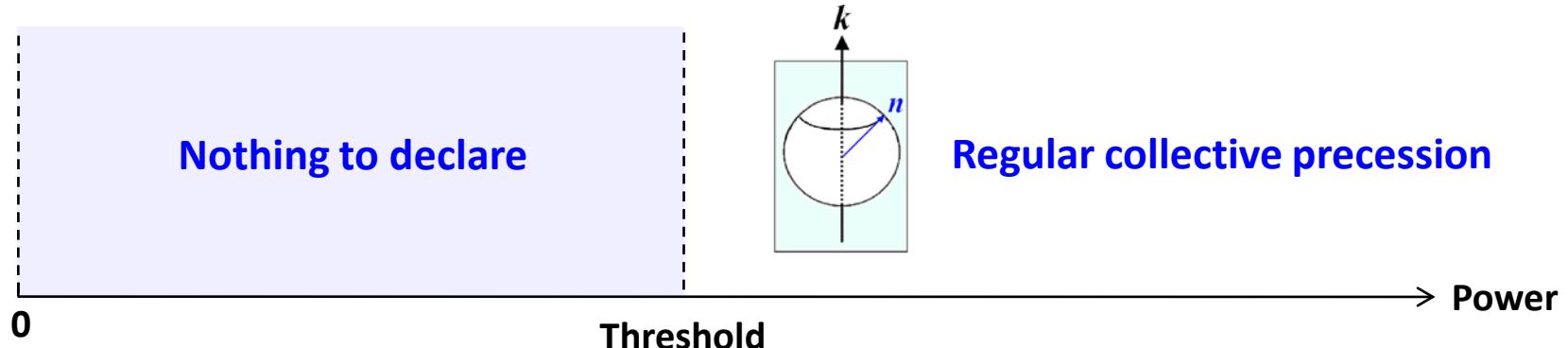


Fixed applied voltage U

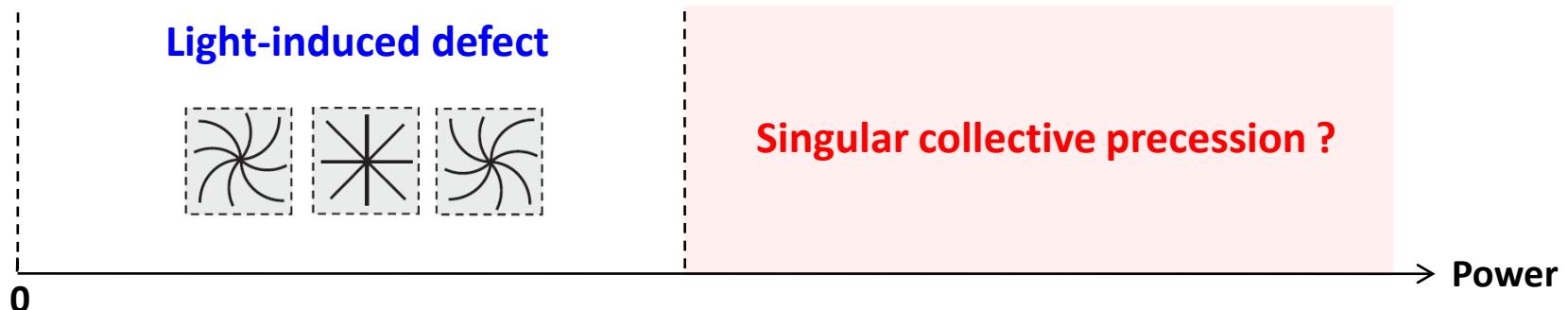


# What about the director precession ?

## Regular optical reorientation



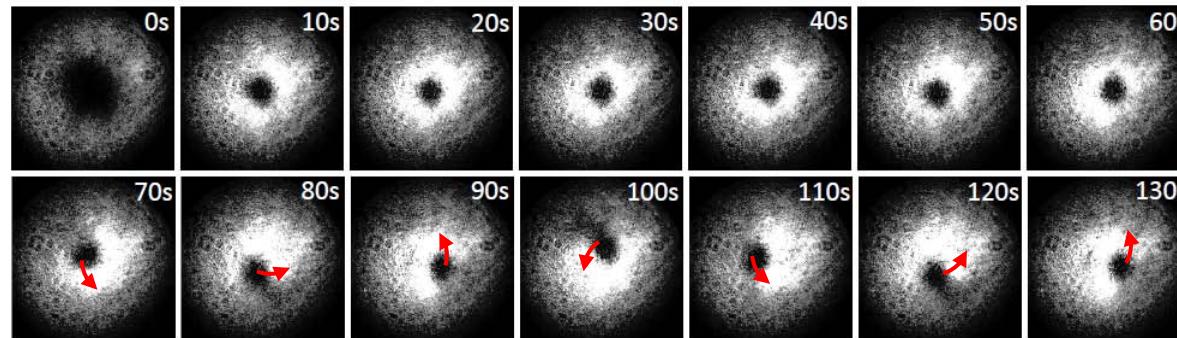
## Singular optical reorientation



# Self-induced optical vortex beam precession

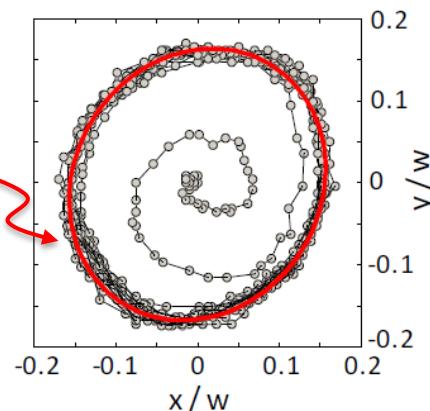
Axial symmetry spontaneously breaks above a threshold

$$P > P_c$$

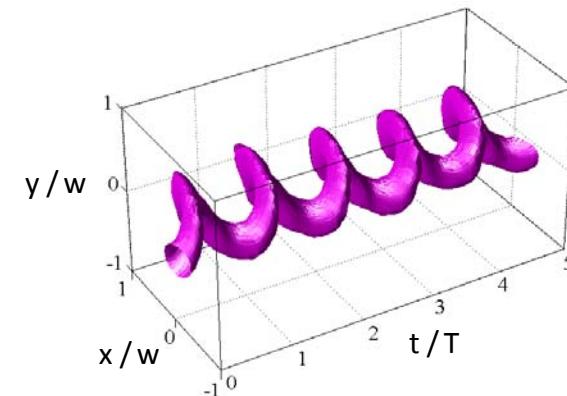


Optical vortex dynamics

Stationary trajectory

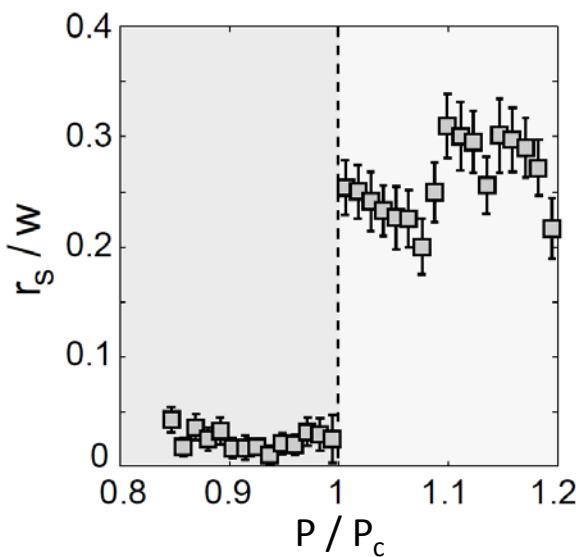


Vortex core dynamics

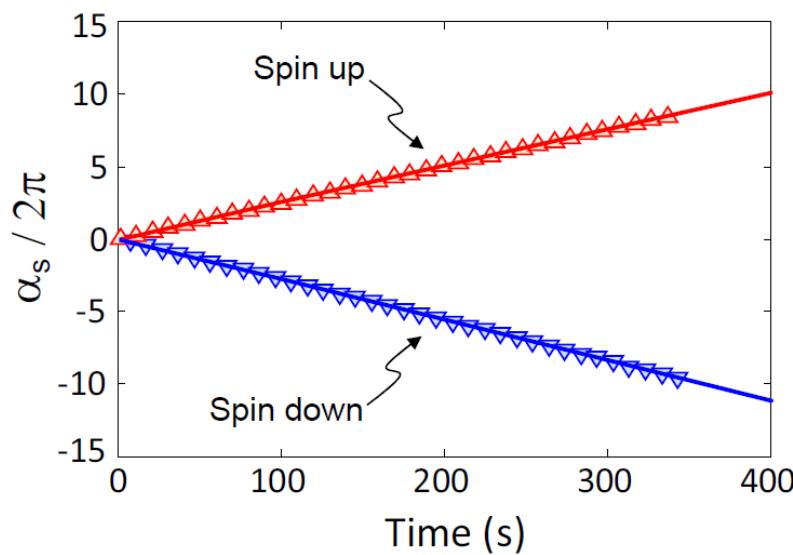


# Characteristics of the phenomenon

Threshold behavior



Spin-dependent orbiting motion



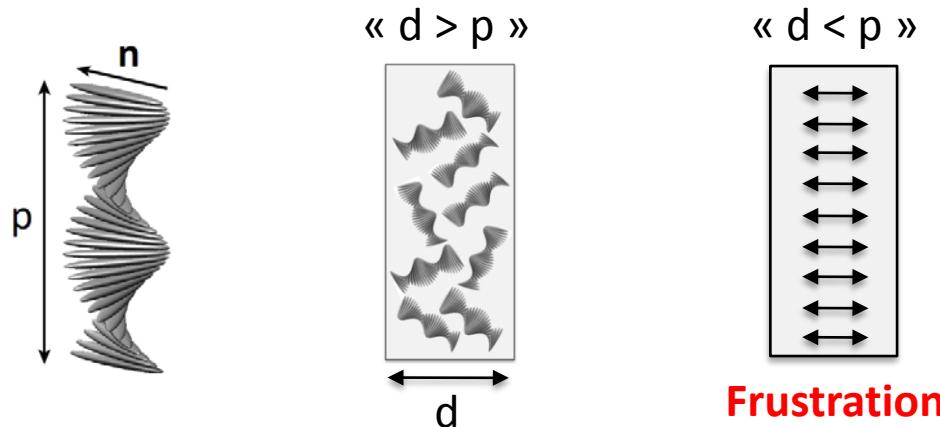
However, all reported effects relax when the beam is turned off ...

# Outline

1. Light-induced liquid crystals topological defects
2. On-demand optical vortex generation
3. Nonlinear spin-orbit optical phenomena
4. **Reconfigurable metastable light-induced vortex arrays**

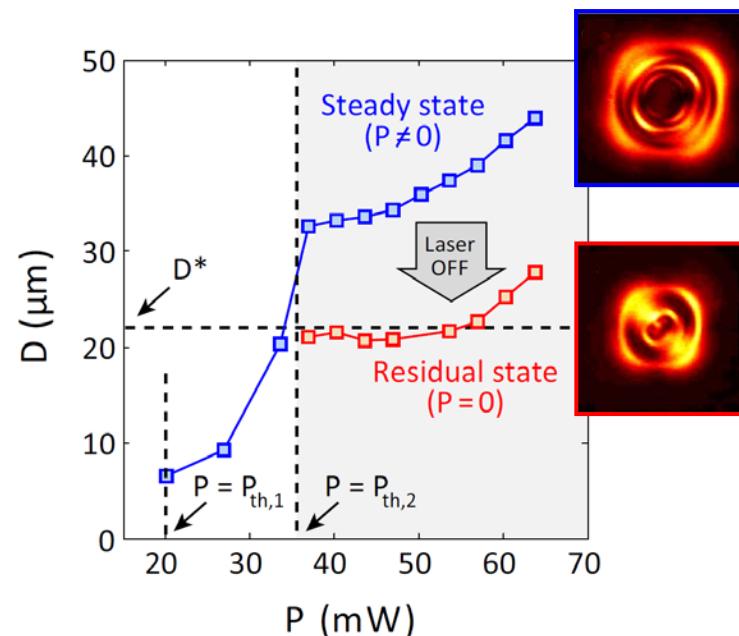
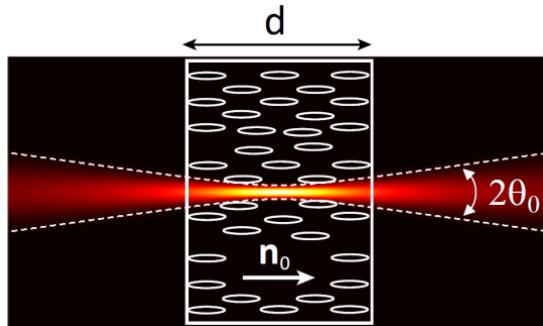
# Laser-induced permanent defects in frustrated cholesterics

## Cholesteric film with perpendicular boundary conditions



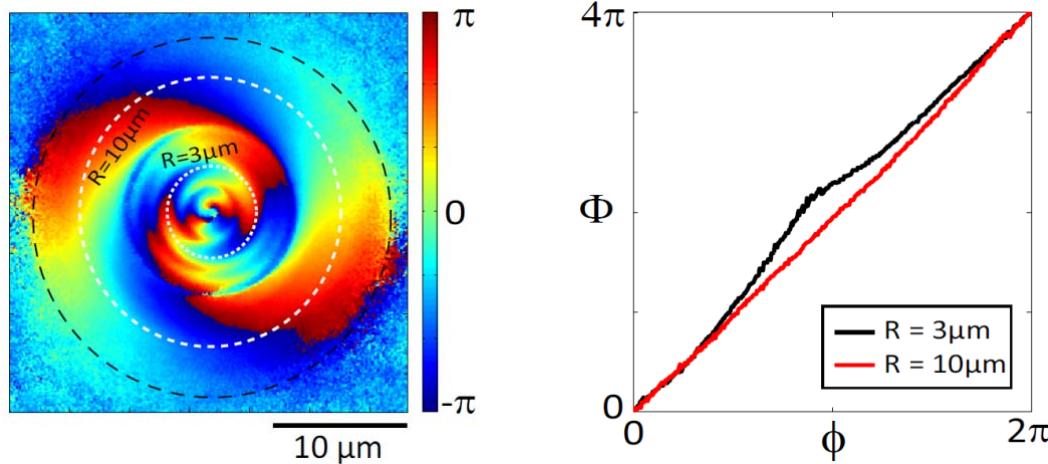
Frustration

## The experiment

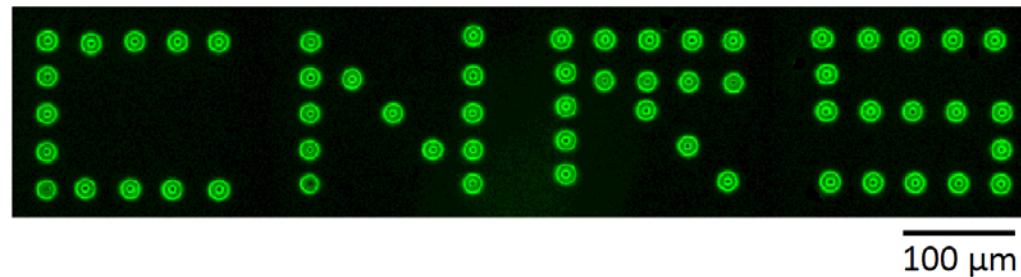


# Arbitrary vortex arrays from optical winding of frustrated cholesterics

## Spin-orbit optical vortex generation

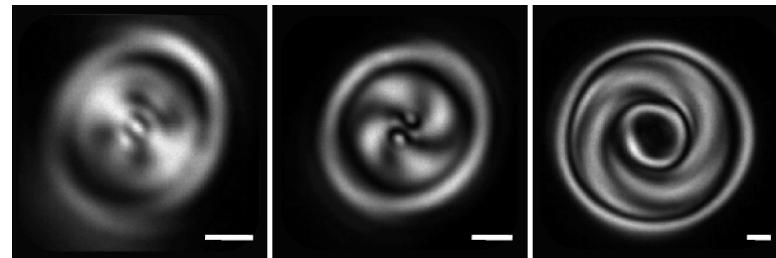


## Switchable arbitrary vortex arrays

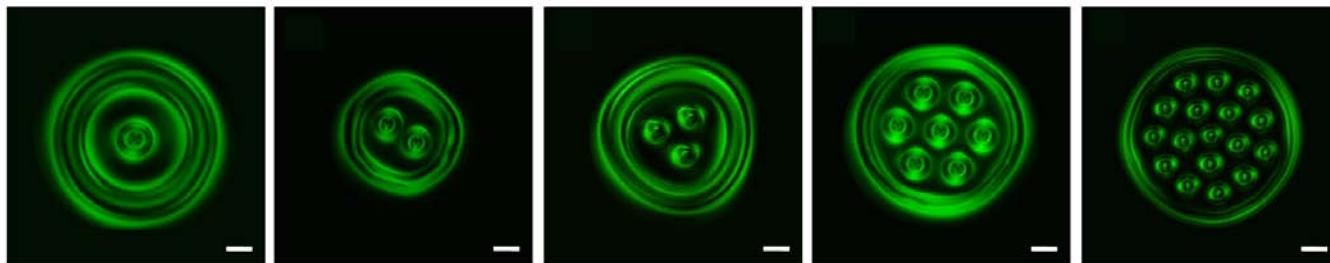


# Frustrated cholesterics under Gaussian beams : topological gallery

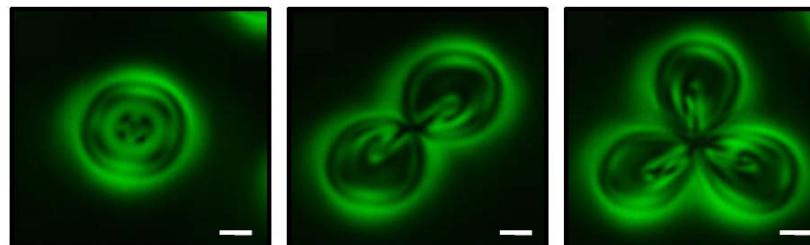
Topological diversity



Topological families

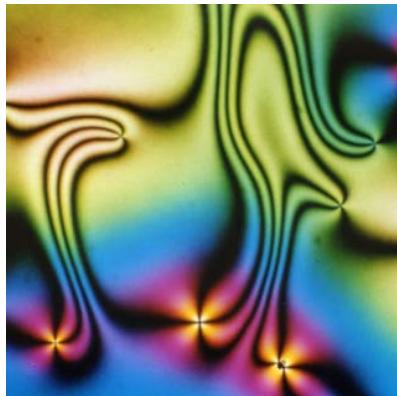


Topological multimers

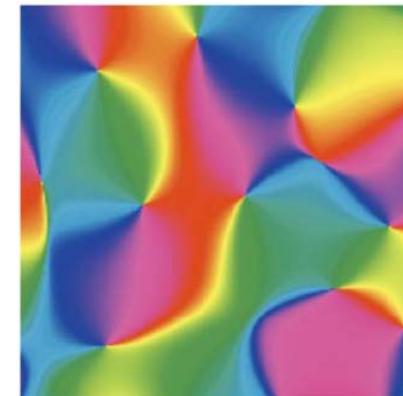


# Matter/Waves interaction in presence of singularities

## Light-induced singular patterning of matter



Spin-orbit interaction



## Matter-induced singular patterning of light

